

## Private Matching

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# Private Matching

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## Abstract

Consider two organizations that wish to privately match data. They want to find common data elements (or perform a join) over two databases without revealing private information. This was the premise of a recent paper by Agrawal, Evfimievski, and Srikant. We show that Agrawal et al. only examined one point in a much larger problem set and we critique their results. We set the problem in a broader context by considering three independent design criteria and two independent threat model factors, for a total of five orthogonal dimensions of analysis.

Novel contributions include a taxonomy of design criteria for private matching, a secure data ownership certificate that can attest to the proper ownership of data in a database, a set of new private matching protocols for a variety of different scenarios together with a full security analysis. We conclude with a list of open problems in the area.

## 1 Introduction

Agrawal, Evfimievski, and Srikant recently presented a paper [1] that explores the following *private matching* problem: two parties each have a database and they wish to determine common entries without revealing any information about entries only found in one database. This paper has generated significant interest in the research community and technical press. While the Agrawal/Evfimievski/Srikant (AgES) protocol is correct within its assumptions, it is not robust in a variety of different scenarios. In fact, in many likely scenarios, the AgES protocol can easily be exploited to obtain a great deal of information about another database. As we discuss

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in this paper, the private matching problem has very different solutions depending on assumptions about the different parties, the way they interact, and cryptographic mechanisms available. Our paper discusses flaws in the AgES protocol, presents that protocol in the context of a framework for viewing private matching and a family of possible protocols, and gives a number of new techniques for addressing private matching, including a flexible powerful Data Ownership Certificate that can be used with a variety of matching protocols.

The private matching problem is a practical, constrained case of the more general (and generally intractable) challenge of *secure multi-party computation*. Private set matching is a simple problem that is at the heart of numerous data processing tasks in a variety of applications. It is useful for relational equijoins and intersections, as well as for full-text document search, cooperative web caching, preference matching in online communities, and so on. Private matching schemes attempt to enable parties to participate in such tasks without worrying that information is leaked.

In this paper we attempt a holistic treatment of the problem of two-party private matching. We lay out the problem space by providing a variety of possible design goals and attack models. We place prior work in context, and present protocols for points in the space that had been previously ignored. We also point out a number of additional challenges for future investigation.

### 1.1 Scenarios

We begin our discussion with three scenarios, which help illustrate various goals of a private matching protocol.

Our first scenario comes from multi-party customer relationship management in the business world. Two companies would like to identify their common customers for a joint marketing exercise, without divulging any additional customers. In this scenario, we would like to ensure that (a) neither party learns more than their own data and the answer (and anything implied by the pair), and (b) if one party learns the results of the match, both parties should learn it. Agrawal, et al. discuss a special instance of this case in their work [1], which they call *semi-honesty*, after terminology used in secure multi-party literature[12]. In particular, the two companies are assumed to honestly report their customer lists (or, more generally, the lists they

wish to intersect), but may try otherwise to discover additional information about the other’s customer list. The semi-honest scenario here rests on the presumption that a major corporation’s publicity risk in being detected lying outweighs its potential benefit in one-time acquisition of competitive information. Below, we comment further on difficulties raised by this notion of semi-honesty.

In many cases, we do not desire symmetric exchange of information. As a second example, consider the case of a government agency that needs to consult a private database. Privacy and secrecy concerns on the part of the government agency may lead it to desire access to the private database without revealing any information about the nature of the query. On the other hand, the database owner may only want to release information on a “need-to-know” basis: it may be required by law to release the answers to the specific query, but may be unwilling to release any other information to the government. In short, a solution to the situation should enable the government to learn only the answer to its query, while the database owner will learn nothing new about the government. In this asymmetric scenario, we need a different choice than (b) above.

Finally, we consider a scenario that could involve anonymous and actively dishonest parties. Online auction sites are now often used as a sales channel for small and medium-sized private businesses. Two competing sellers in an online auction site may wish to identify and subsequently discuss the customers they have in common. In this case, anonymity of the sellers removes the basis for any semi-honesty assumption, so guaranteed mechanisms are required to prevent one party from tricking the other into leaking information.

Each of these examples has subtly different design requirements for a private matching protocol. This paper treats these examples by systematically exploring all possible combinations of privacy requirements along a number of independent design criteria.

## 1.2 Critique of Agrawal, et al.

In their paper [1], Agrawal, Evfimievski, and Srikant consider the first scenario listed above, building on an earlier paper by Huberman et al.[13]. Here is an informal summary of the AgES Set Intersection Protocol result; we discuss it more formally below in Section 3.

Agrawal, et al. suggest solving the matching problem by introducing a pair of encryption functions  $E$  (known only to  $A$ ) and  $E'$  (known only to  $B$ ) such that for all  $x$ ,  $E(E'(x)) = E'(E(x))$ . Alice has customer list  $A$  and Bob has customer list  $B$ . Alice sends Bob the message  $E(A)$ ; Bob computes and then sends to Alice the two messages  $E'(E(A))$  and  $E'(B)$ . Alice then applies  $E$  to  $E'(B)$ , yielding (using the commutativity of  $E$  and  $E'$ ) these two lists:  $E'(E(A))$  and  $E'(E(B))$ . Alice computes  $E'(E(A)) \cap E'(E(B))$ . Since Alice knows the order of items in  $A$ , she also knows the the order of items in  $E'(E(A))$  and can quickly determine  $A \cap B$ .

Two main limitations are evident in this protocol. First,

it is *asymmetric*: if we want both parties to learn the answer, we must trust Alice to send  $A \cap B$  to Bob. This asymmetry may be acceptable or even desirable in some scenarios, but may be undesirable in others.

Second, we find the AgES assumption of *semi-honesty* to be hard to imagine in a real attack scenario. Any attacker who would aggressively decode protocol messages would presumably not hesitate to “spoof” the contents of their queries. If we admit the possibility of the attacker spoofing queries, then the AgES protocol is not required; a simpler hash-based scheme suffices. In this scheme (also suggested by Agrawal, et al.) the two parties hash the elements of their lists  $h(A)$  and  $h(B)$  and then compute the intersection of those two lists of hashes. Later in this paper, we augment this hash-based protocol with an additional mechanism to prevent spoofing as well.

## 1.3 A Broader Framework

Below, we consider a broader framework for thinking about private matching.

First, we break down the protocol design space into three independent criteria :

### Design Criteria

- protocols that leak no information (*strong*) vs. protocols that leak some information (*weak*)
- protocols that protect against spoofed elements (*unspoofable*) vs. protocols that are vulnerable (*spoofable*).
- symmetric release of information vs. asymmetric release (to only one party).

We will also consider two different dimensions for threat models:

### Threat Models

- semi-honest vs. malicious parties
- small vs. large data domains

We discuss the design criteria in more detail in the next section and cover the threat models below in Section 3.

## 2 Problem Statement

We define the *private matching* problem between two parties as follows. Let the two parties Alice and Bob have respective sets  $A$  and  $B$  of objects in some domain  $D$ . Suppose Alice wants to pose a matching query  $Q \subseteq D$  to Bob. We call Alice the *initiator* of the query and Bob the *recipient* of the query. We say  $Q$  is *valid* if  $Q \subseteq A$  and *spoofed* otherwise. A *matching* computes  $P = Q \cap B$  or  $\perp$ ; note that  $\perp$  is a message distinguishable from the set  $\emptyset$ , and can be thought of as a warning or error message.

We elaborate upon the three design criteria for private matching described in the previous section:

- We define a matching protocol to be *unspoofable* if it returns  $\perp$  or  $Q \cap A \cap B$  for all spoofed  $Q$ . Otherwise it is *spoofable*.
- We say that a matching protocol is *strong* if any party can learn only:  $P$ , any information that can be derived from  $P$ , and this party's input to the protocol, and nothing else; otherwise the protocol is *weak* with respect to the additional information learnable.
- We say that a matching protocol is *symmetric* if both parties will know the same information at any point in the protocol. Otherwise it is *asymmetric*.

For each of these three dimensions, a bit more discussion is merited. We begin with the *strong/weak* dichotomy. After executing a protocol, a party can derive information by computing functions over its input to the protocol and the protocol's output. An example of such derived information is that a party can learn something about what is *not* in the other party's set, by examining its input and the query result. Since any information that can be computed in this way is an unavoidable consequence of matching, we use  $P$  to denote both  $P$  and the derived information throughout our paper. Note that weak protocols correspond to the notion of semi-honesty listed above — weak protocols allow additional information to be leaked, and only make sense when we put additional restrictions on the parties — typically, that they be semi-honest. In contrast, strong protocols allow malicious parties to exchange messages. Note further that we could define a variety of levels of weak protocols. For example, we define a *size leaking* weak protocol to be one in which the only information leaked is  $P$ , the size of  $A$  and  $B$ , and information that can be derived from these and a party's input. These size leaking weak protocols will be used later in this paper.

For the *spoofable/unspoofable* dimension, there are scenarios where a protocol that is technically spoofable can be considered effectively to be unspoofable. To guarantee that a protocol is unspoofable, it requires the protocol to detect spoofed queries. Given such a mechanism, either of the following two responses are possible, and maintain the unspoofable property: (a) returning  $\perp$ , or (b) returning  $Q \cap A \cap B$ . When a party lacks such a detection mechanism, it cannot make informed decision as when to return  $\perp$ . However, in some situations, the party may be expected to return the set  $Q \cap A \cap B$  with high probability, regardless of whether the query is spoofed or not. This may happen when it is very difficult to spoof elements. We will give an example of this scenario later.

It is also useful to consider the the issue of symmetry vs. asymmetry for the threat models covered in Section 3. In the semi-honest model, parties follow the protocols properly, and so symmetry is enforced by agreement. However, in a malicious model, the parties can display arbitrary adversarial behavior. It is thus difficult to force symmetry, because one party will always receive the results first. (A wide class of cryptographic work has revolved around “fair

exchanges” in which data is released in a way that guarantees that both parties receive it, but it is not clear if those concepts could be efficiently applied in the private matching application.)

## 2.1 Secure Multi-party Computation

The private matching problem is a special case of the more general problem from the literature called *secure multi-party computation*. We now give a brief introduction to secure multi-party computation in the hope of shedding light on some issues in private matching. In a secure  $m$ -party computation, the parties wish to compute a function  $f$  on their  $m$  inputs. In an *ideal model* where a trusted party exists, the  $m$  parties give their inputs to the trusted party who computes  $f$  on their inputs and returns the result to each of the parties. The results returned to each party may be different. This ideal model captures the highest level of security we can expect from multi-party function evaluation[7]. A secure multi-party computation protocol emulates what happens in an ideal model. It is well-known that no secure multi-party protocol can prevent a party from cheating by changing its input before a protocol starts[12]. Note however, that this cannot be avoided in an ideal model either. Assuming the existence of trapdoor permutations, one may provide secure protocols for any two-party computation [19] and for any multi-party computation with honest-majority[11]. However, multi-party computations are usually extraordinarily expensive in practice, and impractical for real use. Here, our focus is on *highly efficient* protocols for private matching, which is both tractable and broadly applicable in a variety of contexts.

## 3 Threat Models

We identify two dimensions in the threat model for private matching. The first dimension concerns the domain of the sets being matched against. A domain can be *small*, and hence vulnerable to an exhaustive search attack, or *large*, and hence not vulnerable to an exhaustive search attack.

If a domain is small, then an adversary Max can enumerate all the elements in that domain and make a query with the entire domain to Bob. Provided Bob answers the query honestly, Max can learn the entirety of Bob's set with a single query. A trivial example of such a domain is the list of Fortune 500 companies; but note that there are also somewhat larger but tractably small domains like the set of possible social security numbers.

A large uniformly distributed domain is not vulnerable to an exhaustive search attack. We will refer to this type of domain simply as *large* in this paper. An example of such a domain is the set of all RSA keys of a certain length. If a domain is large, then an adversary is limited in two ways. First, the adversary cannot enumerate the entire domain in a reasonable single query, nor can the adversary repeatedly ask smaller queries to enumerate the domain. In this way the adversary is prevented from mounting the attack described above. Second, it is difficult for her to query for an

arbitrary individual value that another party may hold, because each party’s data set is likely to be a negligible-sized subset of the full domain.

The second dimension in the threat model for private matching captures the level of adversarial misbehavior. We distinguish between a semi-honest party and a malicious party [12]. A semi-honest party is honest on its query or data set and follows the protocol properly with the exception that it keeps a record of all the intermediate computations and received messages and manipulates the recorded messages in an aggressively adversarial manner to learn additional information.<sup>1</sup> A malicious party can misbehave in arbitrary ways: in particular, it can terminate a protocol at arbitrary point of execution or change its input before entering a protocol. No two-party computation protocol can prevent a party from aborting after it receives the desired result and before the other party learns the result. Also no two-party computation protocol can prevent a party from changing its input before a protocol starts.

Hence we have four possible threat models: a semi-honest model with a small or large domain, and a malicious model with a small or large domain. In the rest of the paper, we base our discussion of private matching protocols in terms of these four threat models.

### 3.1 Attacks

In this section we enumerate a number of different attacks that parties might try to perform to extract additional information from a database. In the scenarios below, we use the notation  $A$  and  $B$  to denote parties, and  $A$  is trying to extract information from  $B$ ’s database.

- **Guessing attack:** In this attack, the parties do not deviate from the protocol. However,  $A$  attempts to guess values in  $B$ ’s database and looks for evidence that those values occur in  $B$ ’s database. Typically,  $A$  would guess a potential value in  $B$ ’s database, and then look for an occurrence of the hash in  $B$ ’s database. Alternatively,  $A$  could attempt to decrypt values in a search for an encrypted version of a particular potential value in  $B$ ’s database (following the pattern in the AgES protocol.) Because of the limitations of this type of attack, it is best suited when the domain of potential values is small. (A variant of this attack is to try all potential values in the domain, an *exhaustive search attack*.)
- **Guess-then-spoof attack:** In this attack, the parties deviate from the protocol. As in the guessing attack,  $A$  generates a list of potential values in  $B$ ’s database. In the spoofing attack,  $A$  runs through the protocol pretending that these potential values are already in  $A$ ’s database. Thus  $A$  will compute hashes or encrypt, and transmit values as if they really were present in  $A$ ’s database. Because this attack involves a guessing

<sup>1</sup>In the introduction, we argued that semi-honest protocols were unrealistic in many situations. However, for completeness we will consider them here.

element, it is also well suited for small domains of potential database values (e.g. social security numbers, which are only 10 digits long).

- **Collude-then-spoof attack:** In this attack,  $A$  receives information about potential values in  $B$ ’s database by colluding with outside sources. For example, perhaps  $A$  and another database owner  $C$  collude by exchanging their customer lists.  $A$  then executes a spoofing attack by pretending that these entries are already on its list. As in guess-then-spoof attack,  $A$  computes hashes or encryptes, and transmits values as if they were really present in  $A$ ’s database. Since  $A$  is deriving its information from third party sources in this attack, it is suited for both small and large domains of potential database values. (N.B.: we group both the guess-then-spoof attack and the collude-then-spoof attack together as instances of *spoofing attacks*. Spoofing attacks occur in the malicious model; in the semi-honest model they can not occur.)
- **Hiding attacks:** In a hiding attack,  $A$  only presents a subset of its customer list when executing a matching protocol, effectively hiding the unrevealed members. This paper does not attempt to discuss defenses against hiding attacks.

Although we would like to prevent all collusion attacks involving malicious data owners, there are limits to what we can accomplish. For example, if Alice and Bob agree to run a matching protocol, nothing can prevent Bob from simply revealing the results to a third party Charlie. In this case, Bob is acting as a proxy on behalf of Charlie, and the revelation of the results occurs out-of-band from the protocol execution. However, we would like to resist attacks where Bob and Charlie collude to disrupt the protocol execution or use inputs not otherwise available to them.

## 4 Terminology and Assumptions

We assume the existence of *one-way collision resistant hash functions* [16]. A hash function  $h(\cdot)$  is said to be one-way and collision resistant if it is difficult to recover  $M$  given  $h(M)$ , and it is difficult to find  $M' \neq M$  such that  $h(M') = h(M)$ . Let  $\text{SIGN}(\cdot, \cdot)$  be a public key signing function which takes a secret key and data and returns the signature of the hash of the the data signed by the secret key. Let  $\text{VERIFY}(\cdot, \cdot, \cdot)$  be the corresponding public key verification function which takes a public key, data, and a signature and returns **true** if the signature is valid for the data and **false** otherwise. For shorthand, we denote  $\{P\}_{sk}$  as the digital signature signed by the secret key  $sk$  on a plaintext  $P$ . The function  $\text{Find}(\cdot, \cdot)$  takes an element and a set and returns **true** if the element is in the set and **false** otherwise.

The *power function*  $f : \text{Key}\mathcal{F} \times \text{Dom}\mathcal{F} \rightarrow \text{Dom}\mathcal{F}$  where  $f$  defined as follows:

$$f_e(x) \equiv x^e \pmod{p}$$

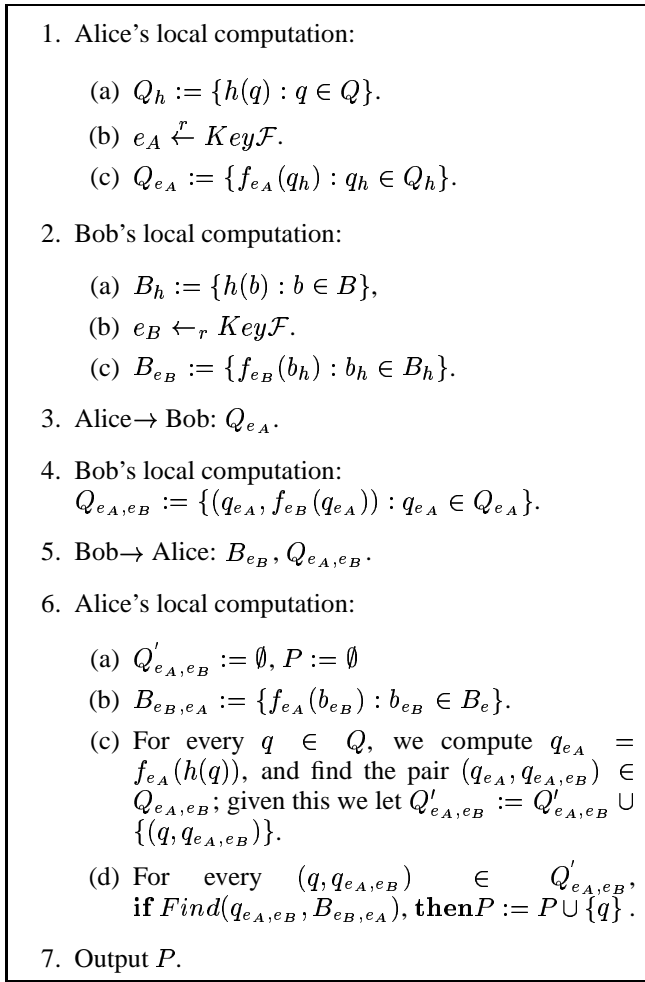


Figure 1: AgES protocol

is a *commutative encryption* [1]:

- The powers commute:

$$(x^d \bmod p)^e \bmod p \equiv x^{de} \bmod p \equiv (x^e \bmod p)^d \bmod p$$

- Each of the powers  $f_e$  is a bijection with its inverse being  $f_e^{-1} \equiv f_{e^{-1} \bmod q}$ .

where both  $p$  and  $q = (p - 1)/2$  are primes.

We use the notation  $e \xleftarrow{r} S$  to denote that element  $e$  is chosen randomly (using a uniform distribution) from the set  $S$ .

We assume there exists an encrypted and authenticated communication channel between any two parties.

## 5 Techniques

We present four matching protocols in this section: the trusted third party protocol, the hash protocol, and the AgES protocol[1]. We also describe a data ownership certificate mechanism that can be combined with all three protocols to *despoof* all of the original protocols even in threat models with small domains.

### 5.1 Trusted Third Party Protocol (TTPP)

Suppose Alice and Bob trust a third party Trudy. Alice and Bob can compute their private matching through Trudy. Alice (resp. Bob) sends her query  $Q$  (resp. his data set  $B$ ) to Trudy, and Trudy computes the intersection  $P$  of the two sets. Trudy then returns the result to both parties in the symmetric case, or to one of the parties in the asymmetric case.

We discuss the security of the TTPP in Section 7.

### 5.2 Hash Protocol (HP)

In this section, we present a *Hash Protocol* that do not require a trusted third party. In the hash protocol, Alice sends Bob her set of hashed values. Bob hashes his set with the same hash function, and computes the intersection of the two sets. Bob may send Alice the result based on their prior agreement.

We discuss the security of the hash protocol in Section 7.

### 5.3 The AgES protocol

We gave a summary of the AgES protocol in Section 1.2. Now we present the complete version of the protocol in Figure 1. For consistency we adapt this protocol to our notation, but the essence of the protocol remains the same as the original paper.

We discuss the security of the AgES protocol in Section 7.

## 6 Data Ownership Certificate (DOC)

An especially difficult attack for private matching to handle is the spoofing problem. In this section, we propose a new approach to address spoofing: the use of *Data Ownership Certificates*. The idea is to have the creator of data digitally sign the data in a particular way so that parties that control databases that include the data can not spoof data. For example, consider the case of two companies each of which wants to find out as much as possible about the other's customer list. If one of the companies has access to a list of all residents in a particular area, a straightforward spoofing attack is quite simple — it could simply create false entries corresponding to a set of the residents. If any of those residents were on the other company's customer list, private matching would reveal their membership on that list. However, if the companies are obligated to provide digitally signed entries, this type of spoofing would be eliminated: neither of the companies would be able to falsify entries.

The above sketch is not sufficient, however, because it still leaves open the possibility that corrupt companies could broker in digitally signed data entries. For example, if customer  $E$  is a legitimate customer of firm  $F$ , we would have the possibility that  $F$  might try to trade or sell  $G$ 's digitally signed entry to  $A$ . Then  $A$  would be able to falsely claim that  $G$  was a customer and during private matching,

steal information through a spoofing attack. Below, we discuss an architecture for data ownership certificates that resists both regular spoofing attacks and colluding spoofing attacks.

Data Ownership Certificates do require more work on the part of individuals creating data, and they are probably only practical in the case of an individual who uses his or her computer to submit information to a database. Despite the extra work involved, we believe that data ownership certificates are not far-fetched. In particular, the European Union’s Privacy Directive[9] requires that individuals be able to verify the correctness of information about them and control how that information is distributed. Data Ownership Certificates give a powerful technical mechanism supporting that distribution. Similarly, Agrawal, Kieran, Srikanth, and Xu have recently argued for a type of ”Hippocratic Database” that would provide similar functionality.[2] Data Ownership Certificates would work well with these Hippocratic Databases.

Now we begin a formal presentation of Data Ownership Certificates (DOC). A Data Ownership Certificate is an authorization token which enables a set owner to prove it is a legitimate owner of some particular data. The first goal of the DOC is to prevent spoofing in a small domain. Data Ownership Certificates prevent spoofing by ’boosting” the size of the small domain  $D$  to a larger domain  $D \times S$ , where  $S$  is the domain of the DOCs. The intuition is that by expanding the domain, DOCs make the probability of guessing a correct value negligible in the cryptographic sense and protect database owners from guess-then-spoof attacks. Now, if an attacker wants to spoof a particular value, e.g. John’s information, the attacker needs to correctly guess the associated DOC as well.

A second goal of Data Ownership Certificates is access control. A DOC is essentially a non-transferable capability issued by the originator of data to a database owner. We refer to the originators of data as *active entities*. We say that an active entity  $E$  *authorizes* a set owner  $O$  *sharing access* to its information  $d$  when  $E$  issues  $O$  a DOC  $C_d^O$  for  $d$ . Ideally, a common element between two databases should be discovered only when both databases have been authorized with DOCs by the corresponding active entity for that element. More precisely, we require two security properties from Data Ownership Certificates:

- Confidentiality: If Bob is not an authorized owner of  $d$ , Bob should not be able to learn that Alice possesses  $d$  if he runs a matching protocol directly with Alice.
- Authenticity: If Bob is not an authorized owner of  $d$  and Alice is an authorized owner of  $d$ , Bob should not be able to pollute Alice’s matching result, i.e., Bob cannot introduce  $d$  into the matching result.

We find that confidentiality is difficult to achieve. We thought of two approaches to do the access control. First, Alice checks whether Bob has the authorization before she gives an element  $v$  to Bob. It seems essential that Alice

obtains some knowledge  $k$  that links the access controlled object  $v$  to requester Bob before granting the access. This requester-specific knowledge  $k$  reveals at least partial information of what element Bob has. It is then only fair that Bob checks for Alice’s permission to access  $k$ . This leads to an infinite reduction. Second, Alice can give Bob a box which contains John’s information  $d$ . The box is locked by John. Bob can only open the box if he has the key. This implies that John uses a lock for which he knows Bob has the key. This kind of precomputation on John’s part is not desirable. We leave this as an open problem for future work and we relax our requirement for access control in this paper. We allow two parties to learn their common element  $d$  if both of them have  $d$  and some *common nonce* for  $d$  instead of some requester specific access token. We refer to the goal of DOC as *reduced confidentiality requirement*.

## 6.1 Our instantiation of Data Ownership Certificates

Our instantiation of Data Ownership Certificates consists of two parts: a common random string and an ownership attestation component. The common random string serves the purpose of both boosting the domain and satisfying the reduced confidentiality requirement. The ownership attestation component satisfies the authenticity requirement.

A Data Ownership Certificate  $C$  has the form of  $\langle pk, n, \sigma \rangle$ . Each active entity  $E$  maintains three keys  $k_1$ ,  $sk$ , and  $pk$ . For each piece of information  $d$  originating from  $E$ ,  $E$  generates a unique  $n = G(k_1 || d)$  where  $G(\cdot)$  is a pseudo-random number generator and  $||$  is the concatenation function. Assume the output  $n$  of  $G(\cdot)$  is  $l$  bits long and  $G(\cdot)$  is cryptographically secure, then by the birthday paradox, one needs to guess approximately  $\sqrt{2^l}$  numbers to have one of them collide with  $n$ . If  $l$  is large enough, say 1024, then guessing the correct  $n$  is hard. This nonce  $n$  will be used in matching protocols instead of the original data  $d$ .

When  $E$  submits  $d$  to some database  $A$ , it generates a signature  $\sigma = \{d || A\}_{sk}$  where  $A$  is the unique ID of the database. The signature does not contain the plaintext information  $d$  or  $A$ , however anyone knowing the public  $pk$  and the plaintext information  $d$  and  $A$  may verify that  $A$  is indeed an authorized owner of  $d$  by verifying the authentication of  $\sigma$  using  $pk$ .

## 6.2 Certified matching protocols

In this section, we describe the integration of Data Ownership Certificates with the proposed protocols from Section 5.

We assume that each set element in database  $A$  is a pair  $(d, C)$  of data and a Data Ownership Certificate  $C = \langle pk, n, \sigma \rangle$  where  $\sigma = \{d || A\}_{sk}$ . A database owner Alice now runs a matching protocol with  $h(n)$  instead of  $d$  as the data.

### 6.2.1 Certified Trusted Third Party Protocol (CTTPP)

We describe how to use Data Ownership Certificates to extend the Trusted Third Party Protocol. Let  $A$  (resp.  $B$ ) be the ID of Alice (resp. Bob). The set that Alice (resp. Bob's) sends to Trudy contains elements in the form of  $(h(n_a), \sigma_a, pk_{n_a})$  (resp.  $(h(n_b), \sigma_b, pk_{n_b})$ ), i.e., triples of a common nonce, ownership attestation component, and the corresponding public key. The nonce  $n_a$  (resp.  $n_b$ ) is associated with elements  $a$  (resp.  $b$ ).

When Trudy finds a matching between two common nonces  $n_a$  and  $n_b$ , she compares the corresponding public keys  $pk_{n_a}$  and  $pk_{n_b}$ . If they are not the same, then it means that Alice and/or Bob spoofed the element and forged the corresponding certificate. Trudy cannot tell which is the case and she simply returns  $\perp$  to both of them. If the corresponding public keys are the same, Trudy runs the verification algorithm on Alice's and Bob's ownership attestation component  $\text{VERIFY}(pk_{n_a}, a || A, \sigma_a) = v_2$  and  $\text{VERIFY}(pk_{n_b}, b || B, \sigma_b) = v_2$  to check whether Alice and/or Bob are authorized owners of the matching value. Trudy will find one of the following three cases to be true:

1.  $v_1 = \mathbf{true}$  and  $v_2 = \mathbf{true}$
2.  $v_1 = \mathbf{true}$  and  $v_2 \neq \mathbf{true}$  or vice versa
3.  $v_1 \neq \mathbf{true}$  and  $v_2 \neq \mathbf{true}$

If Trudy encounters case (1), then she concludes Alice and Bob are the authorized owners of the matching element. She adds the element to the result set and continues with the matching computation. We show why this is the case. Suppose only Bob is the authorized owner of the element associated with  $n_b$ . It is unlikely that Alice spoofs the common nonce  $n_a$  where  $n_a = n_b$  as discussed in Section 6.1. Suppose Alice obtains  $n_a$  and the associated DOC for some other database owner, it is highly unlikely that Alice can generate a public/private key pair that is the same as the key pair for  $n_b$ . By symmetry, it is highly unlikely to be the case that Alice is the authorized owner of the element associated with  $n_a$  and Bob spoofs  $n_b$  or the public/private key pair.

If (2) or (3) is the case, it implies Alice and/or Bob spoofed the nonce and an associated DOC or obtained her/his element from some other authorized owner(s) and spoofed a DOC. Trudy returns  $\perp$  for this case.

If Alice (resp. Bob) did not pose a spoofed query and receives  $\perp$  from Trudy, then she (resp. he) knows that the other party was not honest.

### 6.2.2 Certified Hash Protocol (CHP)

The integration of data ownership certificates with the Hash Protocol is slightly different from that with the Trusted Third Party protocol. We assume that Alice poses a query  $Q_h$  each element of which is in the form of  $\langle h(n_a), \sigma_a \rangle$  where  $\sigma_a = \{a || A\}_{sk_a}$ .

Bob hashes each of his common nonces and checks if it matches one of  $h(n_a)$ . If he discovers a match between

$h(n_a)$  and  $h(n_b)$ , then he assumes that the two corresponding ownership attestation components were signed by the same private key and does the following check. Bob first looks up his copy of the public key  $pk_b$  for  $n_b$  and checks if  $\text{VERIFY}(pk_b, b || A, \sigma_a)$  returns  $\mathbf{true}$ . If it does return  $\mathbf{true}$ , it means that Alice is an authorized owner of  $b$ . Bob may add  $b$  to the result set  $P$  and continue with his matching computation. Otherwise Bob can conclude that Alice is not the authorized owner of  $b$  — she either obtained  $h(n_a)$  and the corresponding certificate from some other authorized owner of  $a$  or she was able to guess  $h(n_a)$  and forged the ownership attestation component. Bob cannot tell which was the case. Now Bob has the following two options: (a) return  $\perp$  to Alice, or (b) continue with the matching computation but omit  $b$  from the final result. Either way the modified protocol satisfies the privacy goal of being unspoofable and it enables parties to detect cheating.

We need to be careful about the usage of hash functions in the Certified Hash Protocols. Consider the following two scenarios. In the first scenario, assume that Alice, Bob, and Charlie are authorized owners of some customer John's information  $d$ . Imagine Alice executes the Certified Hash Protocol with Bob and Charlie and she receives data from Bob and Charlie. If Bob and Charlie use the same hash function, e.g. MD5 or SHA1, then Alice may infer that all three of them have  $d$  after the protocol executions with Bob and Charlie respectively. Alice hashes her own copy of the nonce  $n_d$  associated with  $d$  and discovers  $n_b$  is in the sets that Bob and Charlies sends to her. The second scenario is that both Bob and Charlie are authorized owners of  $d$  but Alice is not. Furthermore, assume Alice does not have a copy of  $d$  and its DOC from some other authorized owner. In this case, Alice may infer that Bob and Charlie share some common information although she does not know what it is.

We propose using an HMAC in the Hash Protocol to prevent the inference problem in the second scenario. An HMAC is a keyed hash function that is proven to be secure as long as the underlying hash function has some reasonable cryptographic strength[4]. An  $\text{HMAC}_k(T) =$

$$h(k \oplus \text{opad}, h(k \oplus \text{ipad}, T))$$

is a function which takes as inputs a secret key  $k$  and a text  $T$  of any length; "opad" and "ipad" are some predetermined padding. The output is an  $l$ -bit string where  $l$  is the output of the underlying hash function  $h(\cdot)$ .

Using HMAC in the Certified Hash Protocol avoids the problem in the second scenario as long as each pair of parties uses a different key every time they run the Certified Hash Protocol. This prevents adversaries from correlating elements from different executions of the Hash Protocol.

### 6.2.3 Certified AgES protocol (CAGES)

We need to modify the AgES protocol in Figure 1 in three ways. First, both Alice and Bob hash and encrypt the common nonce instead of the actual data. Second, Bob returns pairs  $\langle \sigma_b, f_{e_B}(h(n_b)) \rangle$  for each of his encrypted elements

$f_{e_B}(h(n_b))$ . Third, whenever there is a match, Alice verifies whether Bob is an authorized owner by checking the corresponding  $\sigma_b$ .

### 6.3 Homomorphic DOC (HDOC)

The data ownership certificate as proposed is limited in a way that it does not enable authorized set owners to match a subset of the attribute values of an active entity’s information. This *partial matching* property is desirable in many situations. For example, customer database  $A$  is an authorized owner of some customers’ name, credit card number, and mailing address and customer database  $B$  is an authorized owner of the same customers’ name, credit card number and email addresses. Suppose  $A$  and  $B$  wish to find out their common customer by intersecting their respective set of credit card numbers. In our proposed DOC scheme, this is not possible since the common nonce for each of  $A$ ’s customers is generated from names, credit card numbers and email addresses while those for  $B$ ’s customers are generated from names, credit card numbers and email addresses. In this section, we describe a *Homomorphic Data Ownership Certificate* scheme that allows all the databases that are authorized to share information an active entity’s information  $S$  to share any subset of  $S$  where  $S$  is a set of strings.

The semantics for a homomorphic data ownership certificate call for a malleable DOC scheme. Given a DOC  $C_{S_E}^O$  for  $S$  from an active entity  $E$ , we would like the set owner to generate a valid  $\bar{C}_{S'_E}^O$  for  $S'$  where  $S' \subset S$  without the help of  $E$ .

Homomorphic signatures have the right property we are looking for. Let  $\odot$  be a generic binary operator. Intuitively, a homomorphic signature scheme allows anyone to compute a new signature  $\text{Sig}(x \odot y)$  given the signatures  $\text{Sig}(x)$  and  $\text{Sig}(y)$  without the knowledge of the secret key. Johnson et. al introduced basic definitions of security for homomorphic signature systems and proposed several schemes that are homomorphic with respect to useful binary operators[14].

We are interested in the set-homomorphic signature scheme proposed in [14] that supports both union and subset operations. More precisely, the scheme allows anyone to compute  $\text{Sig}(S_1 \cup S_2)$  and  $\text{Sig}(S')$  where  $S' \subseteq S_1$  if he possesses  $S_1, S_2, \text{Sig}(S_1)$  and  $\text{Sig}(S_2)$ .

We now describe our construction for a Homomorphic Data Ownership Certificate (HDOC) scheme. We need to modify both the common nonce and the data ownership component to use the homomorphic signatures. Let  $S$  be a set of strings,  $E$  the active entity that originates  $S$ , and  $sk_S$  the signing key exclusively used for  $S$ . When  $E$  submits its information  $S' \subseteq S$  to database  $A$ , it issues  $A$  an HDOC  $H_{sk_S}^A = \langle pk_S, \text{Sig}_{sk_S}(S'), \text{Sig}_{sk_S}(S \cup A) \rangle$ .

Computing intersection on data with HDOC is straight forward. Suppose databases  $O_1$  and  $O_2$  wish to compute intersection on their customers’ credit card number. Then for each customer  $c_i$ ’s HDOC components  $\text{Sig}_{sk_S}(S_{c_i})$  and  $\text{Sig}_{sk_S}(S_{c_i} \cup O_1)$ , database  $O_1$  computes  $\text{Sig}(S'_{c_i})$  and

Technique		Unspoofable	Strong	Symmetric
TTPP	Sym		X	X
	Asym		X	
HP				
AgES				
CTTPP	Sym	X	X	X
	Asym	X	X	
CHP		X <sup>(1)</sup>	X	

(a) The Malicious Model with a small domain

Technique		Unspoofable	Strong	Symmetric
TTPP	Sym		X	X
	Asym		X	
HP			(*)	
AgES			(*)	
CTTPP	Sym	X	X	X
	Asym	X	X	
CHP		X <sup>(1)</sup>	(*)	

(b) Malicious Model with a large domain

Technique		Unspoofable	Strong	Symmetric
TTPP	Sym	X	X	X
	Asym	X	X	
HP		X		
AgES		X	(*)	
CTTPP	Sym	X	X	X
	Asym	X	X	
CHP		X	X	

(c) The Semi-honest Model with a small domain

Technique		Unspoofable	Strong	Symmetric
TTPP	Sym	X	X	X
	Asym	X	X	
HP		X	(*)	
AgES		X	(*)	
CTTPP	Sym	X	X	X
	Asym	X	X	
CHP		X	(*)	

(d) Semi-honest Model with a large domain

Figure 2: Security goals satisfied by each protocol. (\*): Note that for these examples, we do not have a strong protocol. However, we do have a size leaking weak protocol which only reveals information derivable from the result, the inputs of a given party, and the size of  $A$  and  $B$ . While size leaking protocols are weak, they still limit the amount of information leaked. X<sup>(1)</sup> denotes a protocol is unspoofable in the absence of colluding adversaries.

$\text{Sig}(S'_{c_i} \cup O_1)$  where  $S'_{c_i} = \{c_i's \text{ credit card \#}\}$ .  $O_2$  does similar computations. Then  $O_1$  and  $O_2$  may run any matching protocol as described in Section 6.2 using the HDOC.

## 7 Security Analysis

Recall that we consider four threat models in our paper. They are the malicious model with a large or small domain, and the semi-honest model with a large or small domain.

We have also identified three types of goals a private matching protocol can satisfy: strong/weak, unspoofable/spoofable, and symmetric/asymmetric. In this section, we analyze the effectiveness of the four private matching protocols with respect to each of the threat models and determine what privacy goals each protocol achieves.

### 7.1 The Malicious Model with a Large Domain

We now analyze fulfillment of the security goals of the three protocols. We give a summary of the results in Figure 2(d). Note further that all three protocols are spoofable in the presence of collude-then-spoof attacks. Although a large domain makes it difficult for an adversary to guess a possible element, the adversary can include values obtained from another database in the query to increase the probability of success.

#### 7.1.1 Trusted Third Party Protocol

The Trusted Third Party Protocol (TTPP) is a spoofable, strong and either symmetric or asymmetric matching protocol. TTPP can be either symmetric or asymmetric depending on whether the trusted third party sends query results to one or both parties. TTPP is strong because both parties learn only  $P$  and nothing else in a symmetric setting; in an asymmetric setting, one party learns  $P$  and the other party learns nothing. TTPP is always strong for the same reason in all four threat models.

#### 7.1.2 Hash Protocol

The Hash Protocol is spoofable, weak, and asymmetric. It is leaking weak because the recipient of the data set learns size of it besides the query results  $P$ .

Regardless if the adversary is malicious or semi-honest, the Hash Protocol is always weak since extra information besides the query result is revealed: either the size of the query or the size of the data set.

#### 7.1.3 AgES protocol

The AgES protocol is spoofable, weak, and asymmetric. AgES is weak since the protocol initiator learns the size of the recipient's set and the recipient learns the size of the query. It is asymmetric since the initiator learns the result of the query and the recipient may or may not receive the query result.

### 7.1.4 Certified matching protocols

The CTTTPP is unspoofable. If one of the parties spoofs some element  $d$ , the trusted third party can detect it by checking the ownership attestation component as described in Section 6.2.1.

Both the CHP and the CAgES are unspoofable in the absence of colluding adversaries. The common nonces a DOC prevent a party from guessing the correct nonce associated with certain and thus prevents guess-then-spoof attacks.

When there exists colluding parties, CHP and CAgES are spoofable. Assume Alice colludes with Charlie and Alice obtains data  $d$  and the associated DOC from Charlie. When Bob sends his data set to Alice in an CHP execution, Alice can learn whether Bob has  $d$  or not by hashing the nonce  $n_d$  associated with  $d$  and checks if it is in Bob's set. Similarly, in a CAgES protocol execution, Alice encrypts the nonce  $n_d$  and sends it to Bob. Alice will discover whether Bob has  $d$  or not. On the other hand, if Alice and Bob switch roles in the CHP and CAgES protocol executions, Alice cannot prove to Bob that she has  $d$  since she does not have a valid ownership attestation component for  $d$ .

We present the fulfillment of the goals of the certified trusted third party protocol and the certified hash protocols, and the certified AgES protocol in Figure 2(d) for comparison.

### 7.2 The malicious model with a small domain

With a small domain, a malicious adversary can guess an element of the other party's set with non-negligible probability. An adversary can then launch a spoofing attack and learn elements of the other party's set not contained in its own with non-negligible probability. Therefore, without modification, all three protocols are spoofable in a small domain regardless if the threat model is malicious or semi-honest.

#### 7.2.1 Trusted third party protocol

The trusted third party protocol is strong, spoofable and either symmetric or asymmetric. The analysis is similar to that of the large domain presented in Section 7.1.1.

#### 7.2.2 Hash protocol

The hash protocols are weak, spoofable and asymmetric. The analysis is similar to that of the hash protocol in a large domain presented in Section 7.1.2.

#### 7.2.3 AgES protocol

The AgES protocol is weak, spoofable and asymmetric. AgES is spoofable because although the encryption scrambles the data, it cannot prevent spoofing attacks. The analysis for weak and asymmetric is similar to that of a large domain presented in Section 7.1.3.

Protocol	Cost	
TTPP	$q \log q + b \log q$	$O(b \log b)$
DSHP	$C_h(q + b) + b \log b + q \log b$	$O(b \log b)$
AgES	$(C_h + 2C_e)(q + b) + 2b \log b + 3q \log q$	$O(C_e b)$
CTTPP	$q \log q + b \log q + 2C_x r$	$O(C_x r)$
CDSHP	$C_h(q + b) + b \log b + q \log b + C_x r$	$O(C_x r)$

(a) Computational cost

Protocol	Cost	
Asymmetric TTPP	$(q + b + r) \cdot n$	$O(bn)$
Symmetric TTPP	$(q + b + 2r) \cdot n$	$O(bn)$
DSHP	$b \cdot l$	$O(bl)$
AgES	$(2q + b) \cdot m$	$O(bm)$
Asymmetric CTTPP	$(q + b + r) \cdot n + (q + b) \cdot k$	$O(bn)$
Symmetric CTTPP	$(q + b + r) \cdot n + (q + b) \cdot k$	$O(bn)$
CDSHP	$b \cdot (l + k)$	$O(bk)$

(b) Communication cost

Figure 3: Cost analysis

### 7.2.4 Certified matching protocols

By combining the DOC with TTPP and HP, we obtain protocols that satisfy the same privacy goals in a semi-honest model with small domains as the corresponding protocols in a semi-honest domain with large domains. In particular, by adding a DOC component, we strengthen a protocol to detect spoofed queries to achieve the security goal of being unspoofable. Now the certified version of a protocol satisfies the same privacy goals in a small domain as the unmodified version in a malicious model with large domain. We show these results in Figures 2(d) through 2(c).

### 7.3 The Semi-honest Model with a Small Domain

All the protocols except for the Trusted Third Party Protocol and the AgES Protocol satisfy the same privacy goals in the Semi-honest Model with small domains as they do in the Malicious Model with small domains.

In the semi-honest threat model with a small domain, TTPP is unspoofable, strong, and symmetric/asymmetric. It is unspoofable since both protocol participants are honest about their query or data set and the trusted third party only returns the matching result and nothing else to the participants. The analysis of TTPP being strong and symmetric/asymmetric is similar to that of a large domain presented in Section 7.1.

In the semi-honest threat model with a small domain, AgES is an unspoofable, asymmetric and *size leaking weak protocol* in which the only additional information leaked is the size of the query and the data set. In [1], Agrawal, et al. proved that in the semi-honest threat model, the initiator learns the intersection and the size of the recipient's set.

The recipient learns only the size of the initiator's set.

#### 7.3.1 Certified Matching Protocols

By combining the DOC with TTPP and HP, we obtain protocols that satisfy the same security goals in the malicious threat model with a small domain as in the malicious threat model with a large domain. The analysis is similar to that of the certified matching protocols in the semi-honest model with a small domain.

### 7.4 The Semi-honest Model with a Large Domain

The analysis for the semi-honest model with a large domain is similar to that of the semi-honest model with a small domain. The only difference is that the HP is size leaking weak in the large domain and weak in the small domain.

## 8 Cost Analysis

In this section, we use the following notations. Alice poses a query  $Q$  to Bob who has a set  $B$ . Let  $P = Q \cap B$  be the query result. Let  $q = |Q|$ ,  $b = |B|$ , and  $p = |P|$ . Let  $C_h$  be the cost of hashing and  $C_x$  be the cost of running the public key verification algorithm  $\text{VERIFY}(\cdot, \cdot, \cdot)$ . Let  $j$  be the length of a public key,  $k$  be the length of the ownership attestation component,  $l$  be the length of the output of  $h(\cdot)$ ,  $m$  be the length of each encrypted code word in the range of  $\mathcal{F}$ , and  $n$  be the length of each element; all quantities are in bits. We assume that the set  $Q$  is larger than the set  $B$ , i.e.  $b < q$ , and we assume that  $l \leq k + j \leq n$ .

We present the computational and communication cost in Figure 3(a) and Figure 3(b) respectively.

The computational costs of the trusted third party and hashing protocols are dominated by the cost of sorting the list. For the AgES and certified protocols, the computation cost is dominated by the encryption/decryption and public key signature verification respectively. Further details can be found in Figure 3.

As we may see from Figure 3(b), the communication cost for any proposed protocol is linear in the size of the sets being sent. This linear communication cost is the lower bound of any set intersection protocols which compute the exact matching[15].

## 9 Related Work

Private Information Retrieval (PIR) schemes allow a user to retrieve the  $i$ -th bit of an  $n$ -bit database without revealing  $i$  to the database [8, 6, 3]. These schemes guarantee user privacy. Gertner et al. introduce Symmetrically-Private Information Retrieval (SPIR) where the privacy of the data, as well as the privacy of the user is guaranteed[10]. In every invocation of a SPIR protocol, the user learns only a single bit of the  $n$ -bit database, and no other information about the data. Practical solutions are difficult to find since the PIR literature typically aims for very strong information-theoretic security bounds.

There has been recent work on searching encrypted data [5, 18] inspired by Song, Wagner, and Perrig's original paper describing practical techniques for searching encrypted data[17]. Song et al. proposed a cryptographic scheme to allow a party  $C$  to encrypt and store data on an untrusted remote server  $R$ .  $R$  can execute encrypted queries issued by  $C$  and return encrypted results to  $C$ .

## 10 Future Work

This paper explores some issues associated with private matching. But many areas remain to be explored. Here, we list a few particularly interesting challenges:

- In this paper, we examined two party protocols. What are the issues that arise with more complicated protocols with more than two parties?
- There is a basic asymmetry that arises between two parties where one party knows significantly more than a second party. Parties that control large sets may be able to extract significantly more interesting information than parties that control small sets. There may be instances where parties controlling small sets can detect and reject these queries.
- Here, we only consider examples of matching elements from two sets. More interesting and more far-ranging examples are possible. For instance, this paper considered *listing queries* — we actually listed all the elements held in common between two sets. We can consider a broader range of *functional queries* which return a function calculated over the intersection of two sets. While a broad literature in statistical

databases exists, the question of functional operations is a more general notion that deserves further attention.

- There is an interesting connection between our spoofing discussion and the database literature on updates through views. The view update literature provides (constrained) solutions for the following: given a query on relation instances  $R$  and  $S$  resulting in a set  $P$ , what changes to  $R$  and  $S$  could produce some new answer  $P'$ ? The reasoning used to address that problem is not unlike the reasoning used to learn information via spoofing: by substituting  $R'$  for  $R$  and observing the query result  $P'$ , what can be learned about  $S$ ? The literature on updates through views is constrained because it seeks scenarios where there is a unique modification to  $R, S$  that can produce  $P'$ . By contrast, much can be learned in adversarial privacy attacks by inferring a non-unique set of *possible* values for  $S$ .
- In large distributed systems, it may be desirable to have a set of peer systems store information in a variety of locations. In this broader distributed system, can we still guarantee privacy properties.
- In our list of attacks in Section 3.1, we discussed a hiding attack where a database owner pretends certain values don't occur in its database. Can we provide effective defenses against hiding attacks?

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